

Partial solutions for 5 6 8 11 13 14 39-41

5.  $\lim_{(x,y) \rightarrow (3,2)} f(x,y) = 56$

6.  $\lim_{(x,y) \rightarrow (2,-1)} f(x,y) = -2/3$

8.  $\lim_{(x,y) \rightarrow (3,2)} f(x,y) = e^2$

11. Along  $y = 0$ ,  $\lim_{x \rightarrow 0} f(x, 0) = 0$ . Along  $x = 0$ ,  $\lim_{y \rightarrow 0} f(0, y) = 0$ . Along  $y = x$ ,  $\lim_{x \rightarrow 0} f(x, x) = 1/2$ . Limit does not exist.

13. Hint:  $0 \leq \left| \frac{xy}{\sqrt{x^2 + y^2}} \right| \leq |x|$ . Final:  $\lim_{(x,y) \rightarrow (0,0)} f(x,y) = 0$

14. Factor to get  $f(x,y) = x - y$ . Final: 0

39. Convert to polar.  $\lim_{r \rightarrow 0} r \cos^3 \theta + r \sin^3 \theta = 0$

40. Cover to polar. Need L'Hospital. Final: 0

41. Convert to polar. Need L'Hospital. Final: -1