

4 Techniques of Integration

4.1 Review of Integrals

$$\begin{aligned}\int x^n dx &= \frac{x^{n+1}}{n+1} & \int \frac{1}{x} dx &= \ln|x| \\ \int e^x dx &= e^x & \int a^x dx &= \frac{a^x}{\ln a} \\ \int \sin(x) dx &= -\cos(x) & \int \csc^2(x) dx &= -\csc(x) \\ \int \cos(x) dx &= \sin(x) & \int \csc(x) \cot(x) dx &= -\csc(x) \\ \int \sec^2(x) dx &= \tan(x) & \int \cot(x) dx &= \ln|\sin(x)| \\ \int \sec(x) \tan(x) dx &= \sec(x) & \int \tan(x) dx &= \ln|\sec(x)| \\ \int \frac{1}{x^2+1} dx &= \tan^{-1}(x) & \int \frac{1}{\sqrt{1-x^2}} dx &= \sin^{-1}(x) \\ \int \frac{1}{a^2+x^2} dx &= \frac{1}{a} \tan^{-1}\left(\frac{x}{a}\right)\end{aligned}$$