

Directions: Show all work on a separate sheet of paper for full credit.

1. Use the Laws of Logarithms to expand the quantity $\ln \sqrt[3]{\frac{x-1}{x+1}}$.
2. Express the quantity as a single logarithm: $2 \ln(x) + 3 \ln(y) - \ln(z)$.
3. Simplify the expression $e^{\ln(\ln(e^3))}$.
4. Find the limit.

a) $\lim_{x \rightarrow \infty} e^{-x^2}$

b) $\lim_{x \rightarrow \infty} e^{-2x} \cos(x)$

c) $\lim_{x \rightarrow \infty} [\ln(2+x) - \ln(1+x)]$

5. Differentiate the function.

a) $f(x) = x \ln(x) - x$

b) $f(x) = \sin(\ln(x))$

c) $f(x) = \ln(\sin^2(x))$

d) $f(y) = \ln \frac{(2y+1)^5}{\sqrt{y^2+1}}$ (Hint: try to expand using laws of logarithms first)

e) $f(x) = \ln(\ln(\ln(x)))$

f) $f(x) = \ln(\csc(x) - \cot(x))$

g) $f(x) = e^x + x^e$

h) $y = \frac{e^x}{1 - e^x}$

i) $f(t) = \sin(e^{3t^2})$

j) $f(x) = e^{x \sin(2x)}$

k) $f(x) = x^2 e^{-1/x}$

6. Use logarithmic differentiation to differentiate

a) $y = (x^2 + 2)^2 (x^4 + 4)^4$

b) $y = \sqrt{\frac{x-1}{x^4+1}}$

7. Evaluate the integral.

a) $\int_0^3 \frac{dx}{5x+1}$

b) $\int_4^9 \left(\sqrt{x} + \frac{1}{\sqrt{x}} \right)^2 dx$

c) $\int \frac{dx}{x \ln(x)}$

d) $\int \frac{\cos(\ln(t))}{t} dt$

e) $\int_0^1 (x^e + e^x) dx$

f) $\int e^{\tan(x)} \sec^2(x) dx$

g) $\int \frac{(1+e^x)^2}{e^x} dx$